

Continual Learning Through Synaptic Intelligence

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Joint work with

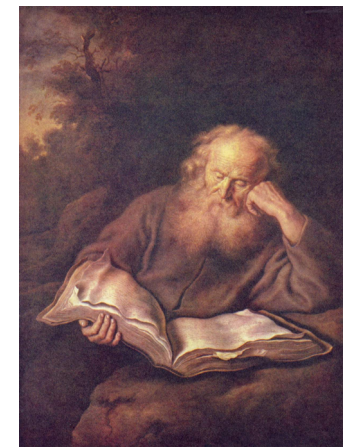
Ben Poole
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Poster: #46



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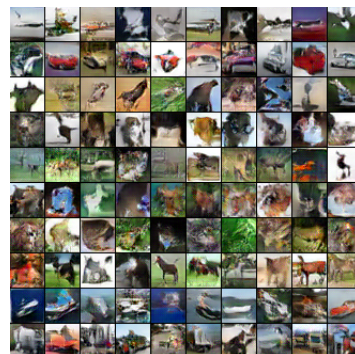
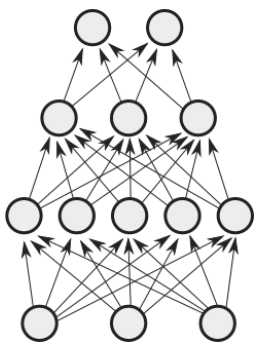
Humans learn continually

Humans: Continual learning, non stationary data



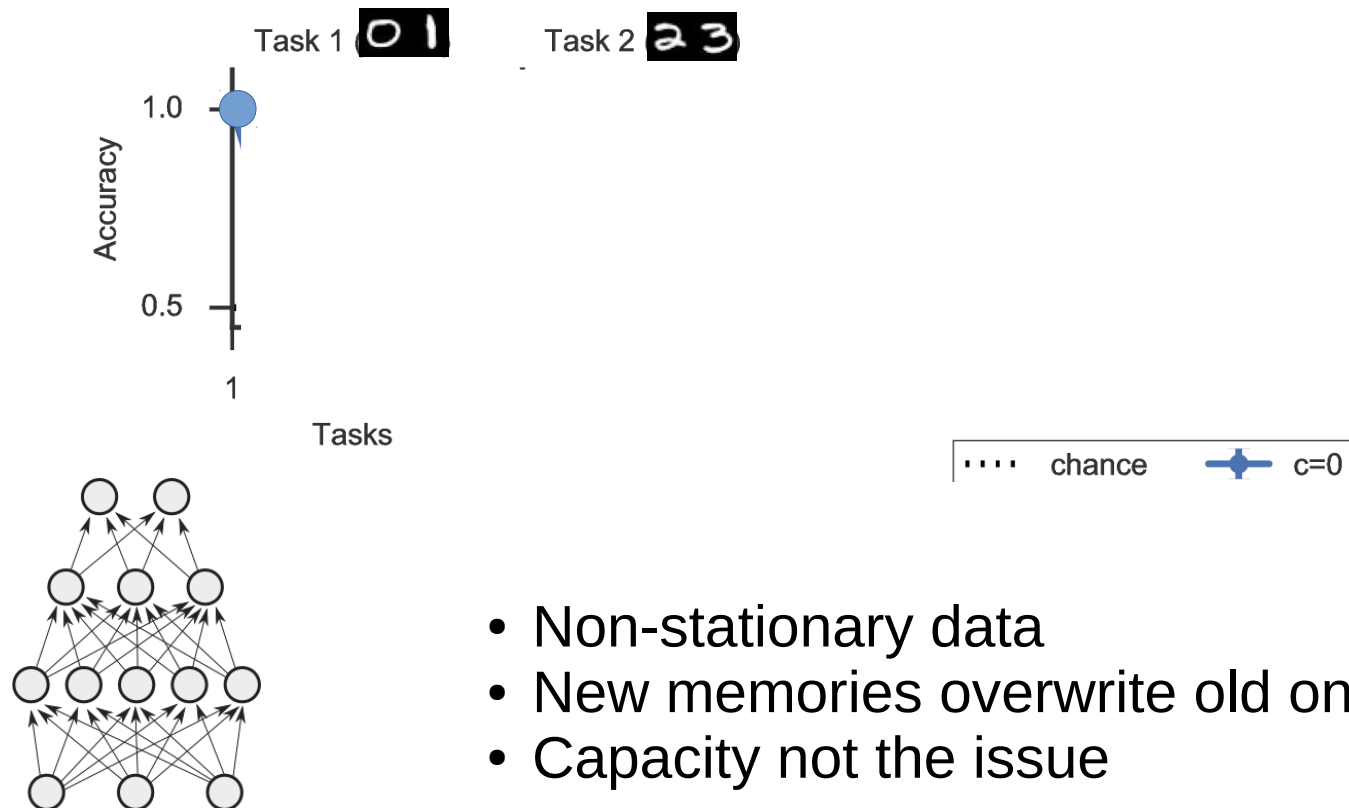
L Muntz, 1898
J-H Fragonard, 1770
S Koninck, 1643

Machines: Training phase, stationary data



Training phase

Problem: Catastrophic forgetting

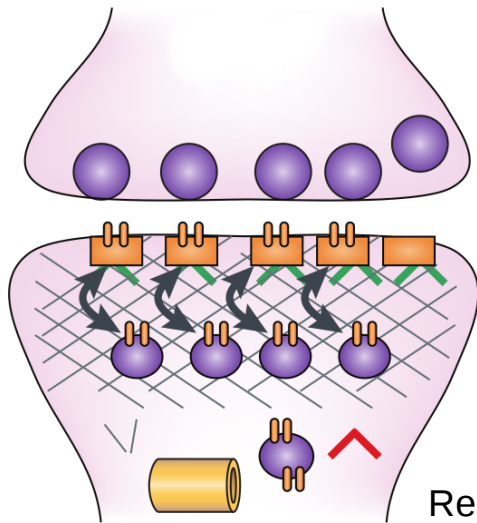


- Non-stationary data
- New memories overwrite old ones
- Capacity not the issue

Synapses, biology's “model parameters”, are complex

Biology: Synapse

Complex biochemical dynamical system



- High-dimensional state space
- Non-linear dynamics on different timescales

Redondo & Morris (2010)

Machines: Parameter

Single scalar value

W or $\theta, J, \dots$

- Individual parameter one-dimensional state space

Computational neuroscience

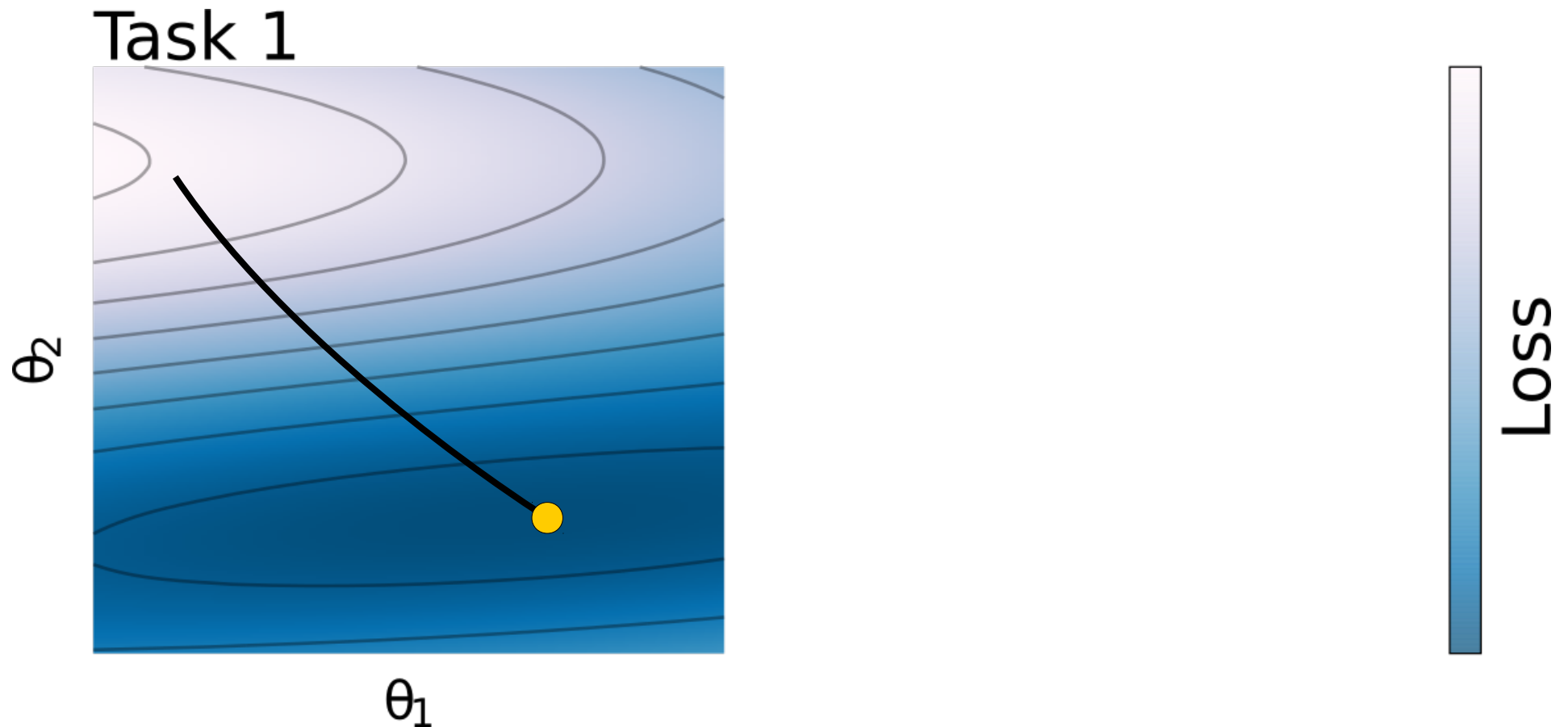
Synaptic complexity is good for continual learning

- Fusi et al. (2005)
- Lahiri & Ganguli (2013)
- Benna & Fusi (2016)

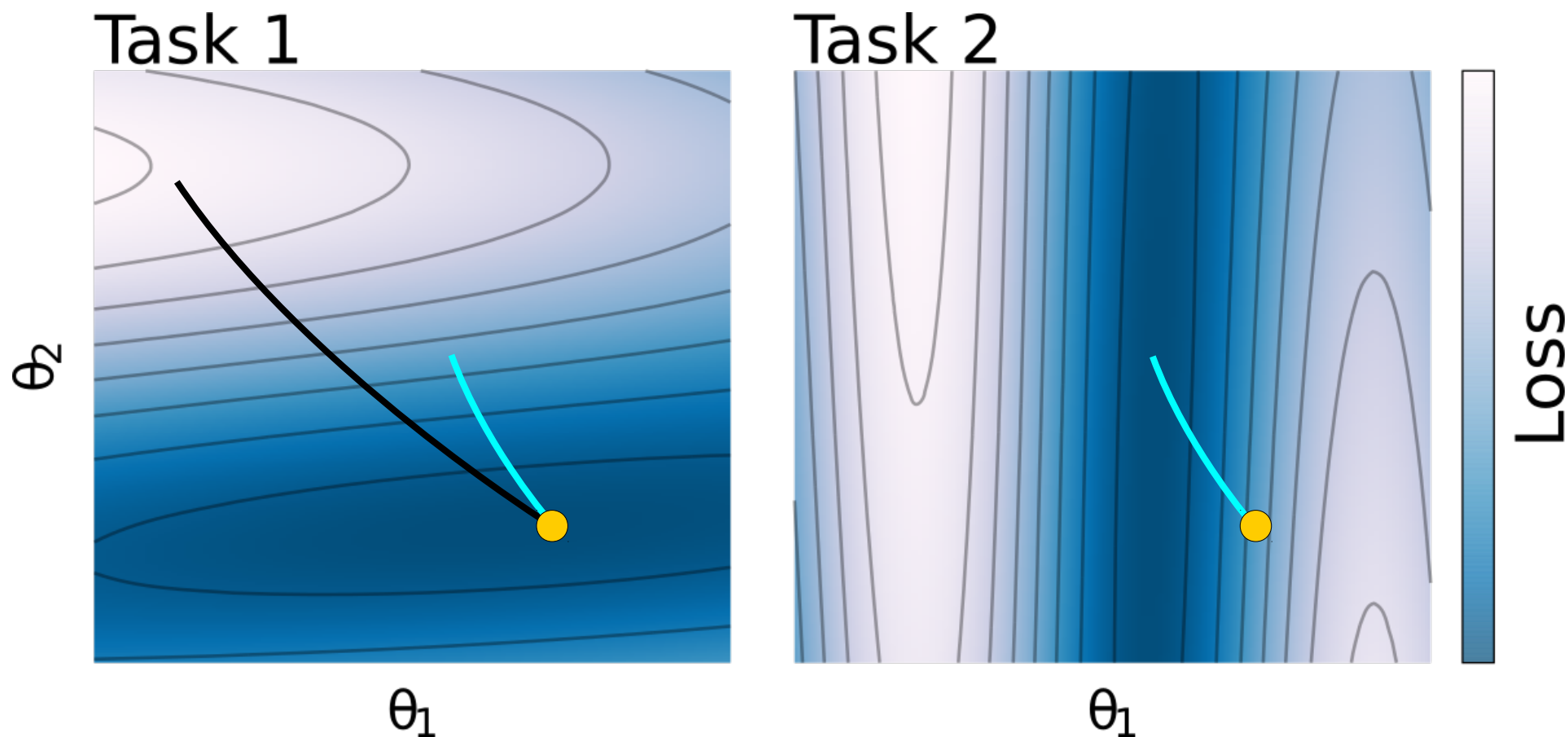
Existing approaches to alleviate catastrophic forgetting

- **Architectural:** Modify architecture
Use specific nonlinearities (Goodfellow et al., 2013; Srivastava et al., 2013), Progressive Nets (Rusu et al., 2016), Fine tuning (Donahue et al., 2014)
- **Functional:** Regularize activations or outputs of network
Learning without Forgetting (Li & Hoiem, 2016), Less-forgetting Learning (Jung et al., 2016)
- **Structural:** Regularize parameters of network
Elastic weight consolidation (Kirkpatrick et al., 2017)

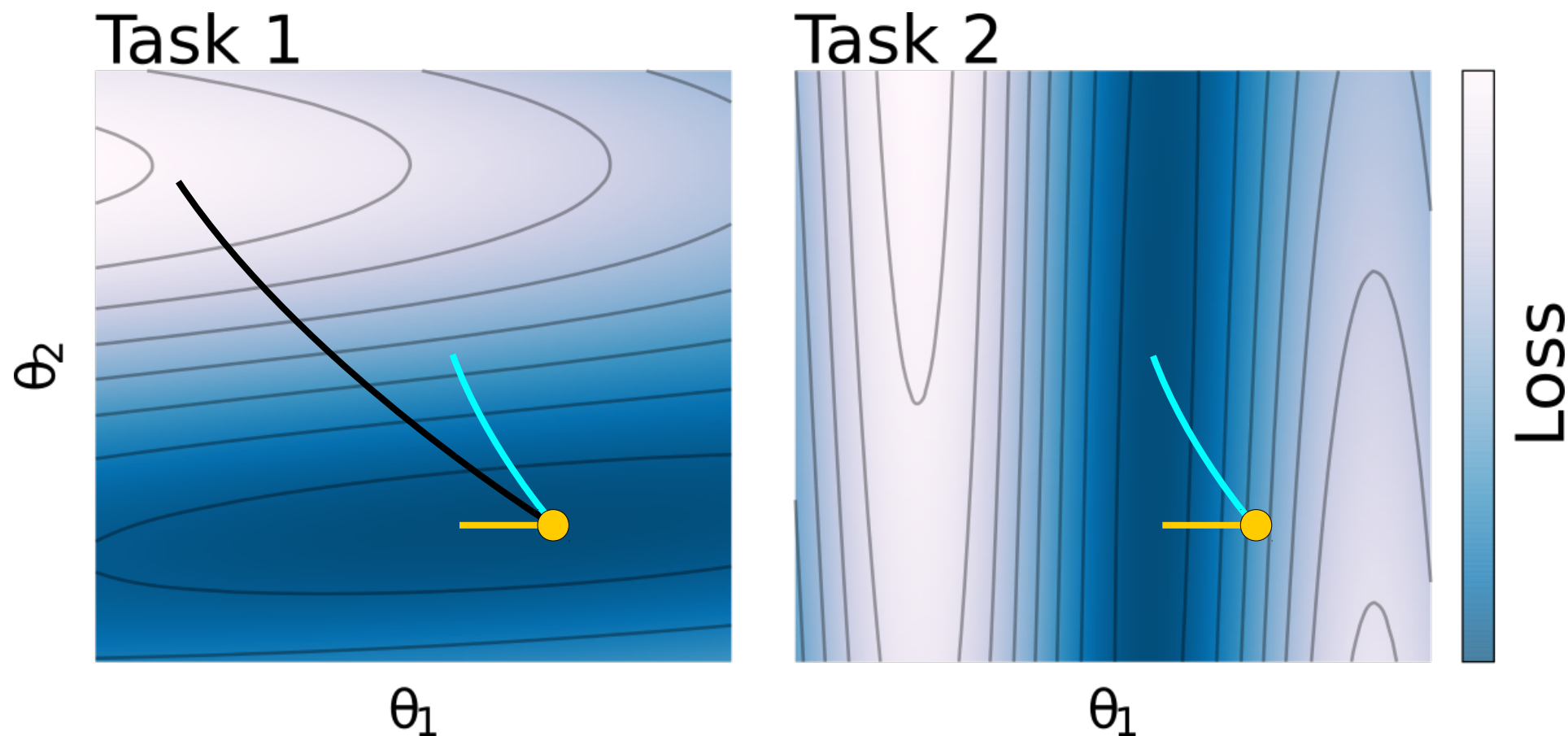
Problem: Catastrophic forgetting



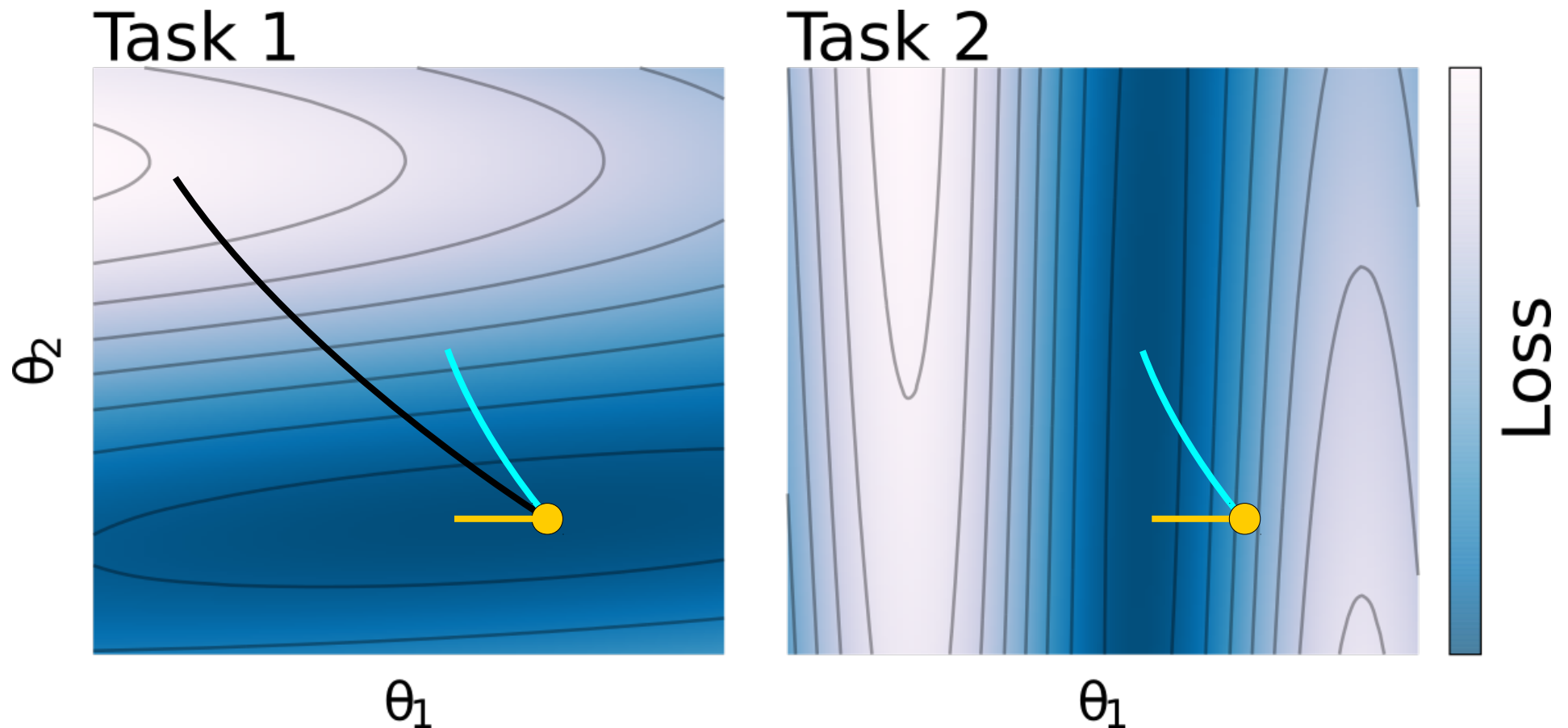
Problem: Catastrophic forgetting



Problem: Catastrophic forgetting



Problem: Catastrophic forgetting



Elastic Weight Consolidation (EWC)

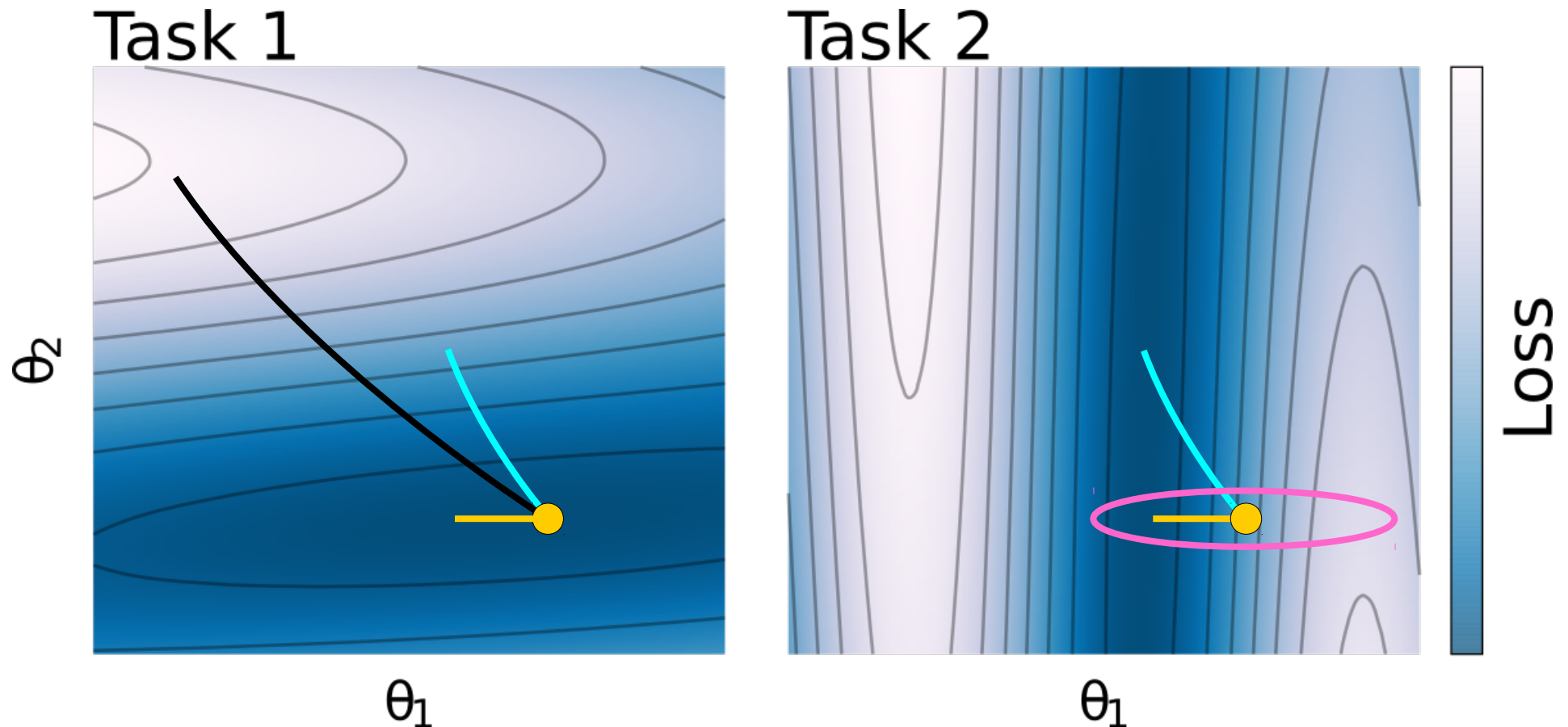
$$L(\theta) = L_2(\theta) + \sum_i \frac{\lambda}{2} F_i (\theta_i - \theta_{1,i}^*)^2$$

- Idea: Approximate $L_1(\theta)$ with quadratic penalty term
 - Each parameter “remembers” its previous value $\theta_{1,i}^*$
 - ... and a local measure of curvature of $L_1(\theta)$

Elastic Weight Consolidation (EWC)

$$L(\theta) = L_2(\theta) + \sum_i \frac{\lambda}{2} F_i(\theta_i - \theta_{1,i}^*)^2$$

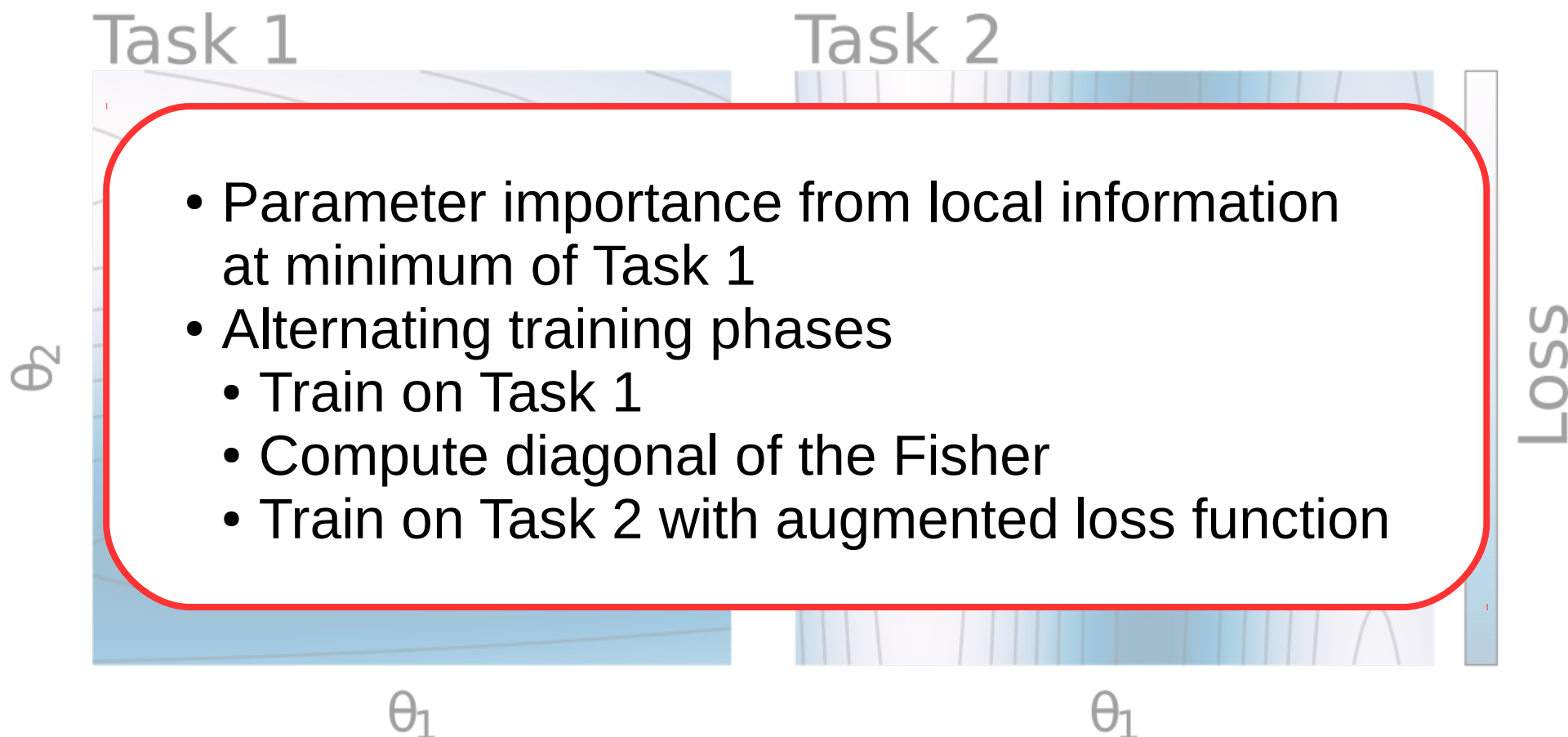
Diagonal of Fisher at ● on Task 1



Elastic Weight Consolidation (EWC)

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Diagonal of Fisher at ●

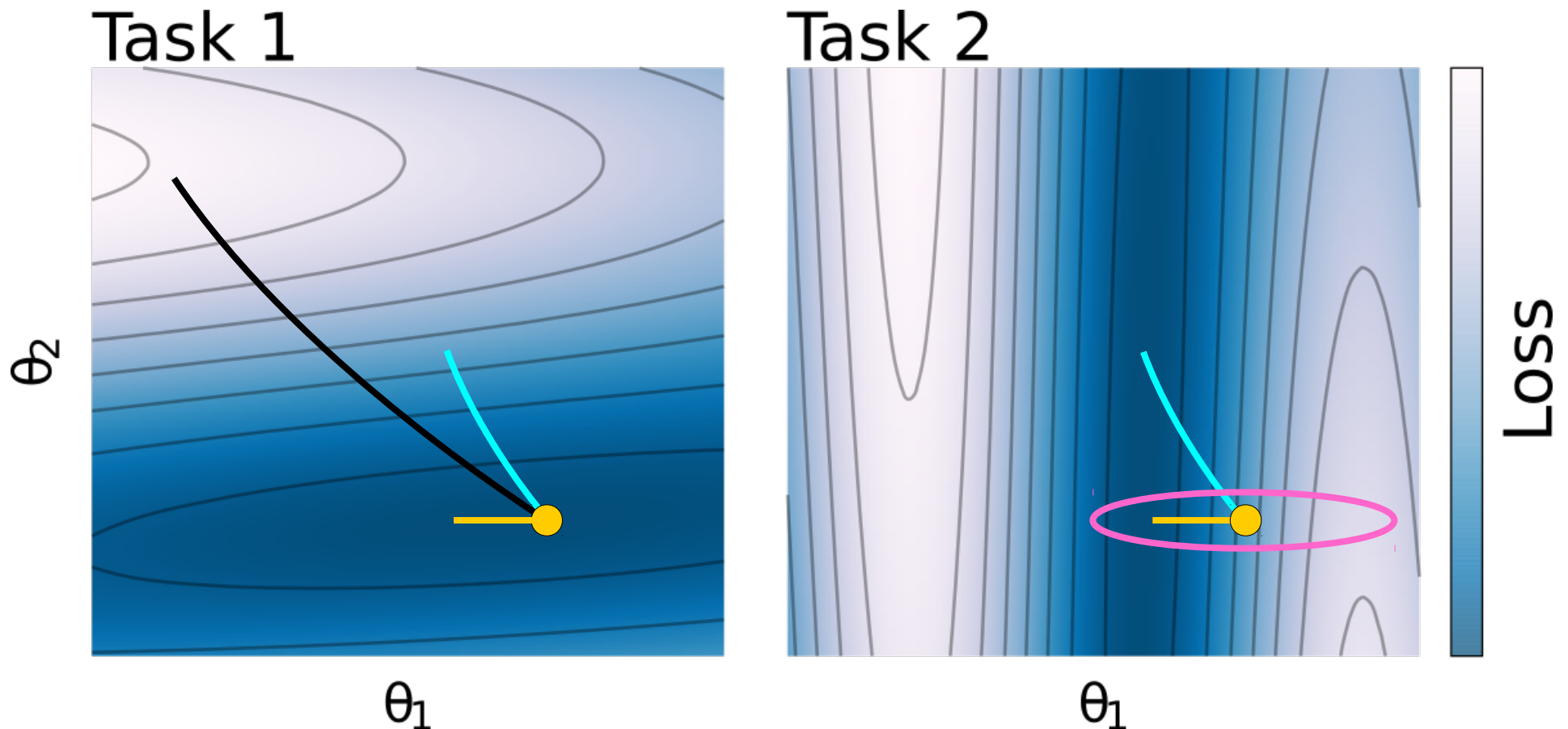


Our Contribution

Our approach: Parameter importance on-line from learning trajectory

$$L(\theta) = L_2(\theta) + c \sum_i \Omega_i (\theta_i - \theta_{1,i}^*)^2$$

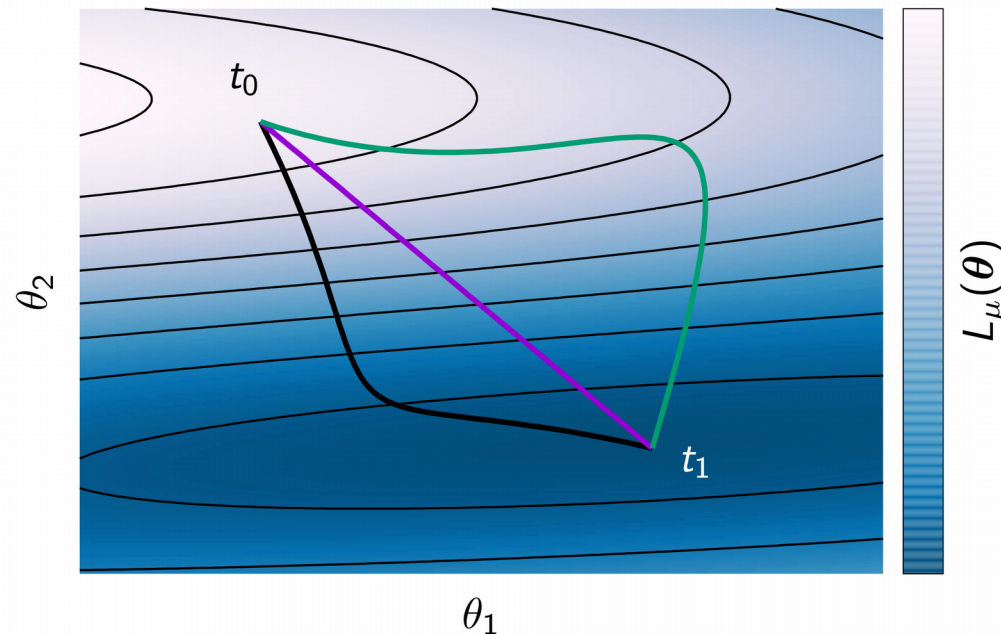
From learning trajectory



Total change in loss is given by the path integral over the gradient field

$$\begin{aligned}\int_C \mathbf{g}(\boldsymbol{\theta}(t)) d\boldsymbol{\theta} &= \int_{t_0}^{t_1} \mathbf{g}(\boldsymbol{\theta}(t)) \cdot \boldsymbol{\theta}'(t) dt = L(t_1) - L(t_0) \\ &= \sum_k \int_{t_0}^{t_1} g_k(t) \theta'_k(t) dt \equiv - \sum_k \omega_k\end{aligned}$$

$\mathbf{g}$: Gradient
 $\boldsymbol{\theta}$: Parameters
 $\boldsymbol{\theta}'$: Updates



Total change in loss is given by the path integral over the gradient field

$$\int_C \mathbf{g}(\boldsymbol{\theta}(t)) d\boldsymbol{\theta} = \int_{t_0}^{t_1} \mathbf{g}(\boldsymbol{\theta}(t)) \cdot \boldsymbol{\theta}'(t) dt = L(t_1) - L(t_0)$$

$$= \sum_k \underbrace{\int_{t_0}^{t_1} g_k(t) \theta'_k(t) dt}_{\omega_k} \equiv - \sum_k \omega_k$$

- Is a parameter-specific quantity
- Can be computed on-line during training (running sum)

Natural way of assigning credit for a global change to local parameters

$$L(t_1) - L(t_0) = - \sum_k \omega_k^\mu$$

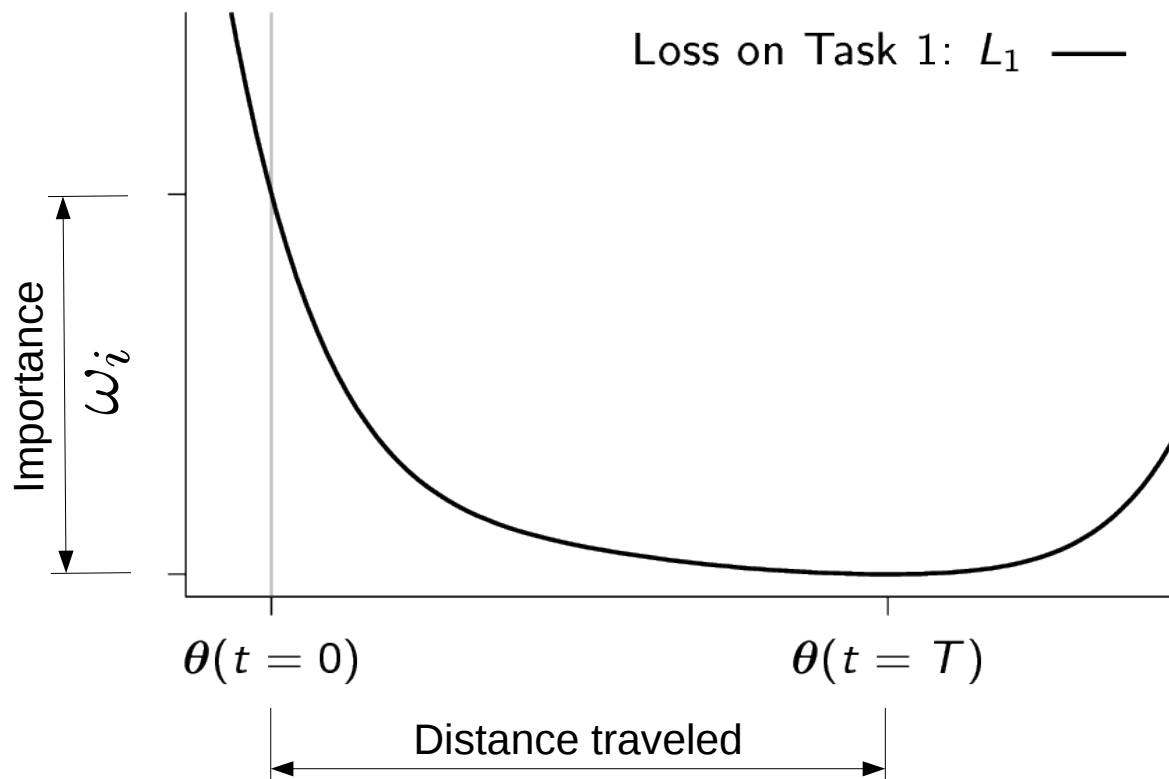
$\mathbf{g}$: Gradient

$\boldsymbol{\theta}$: Parameters

$\boldsymbol{\theta}'$: Updates

Leveraging per-parameter importance for continual learning

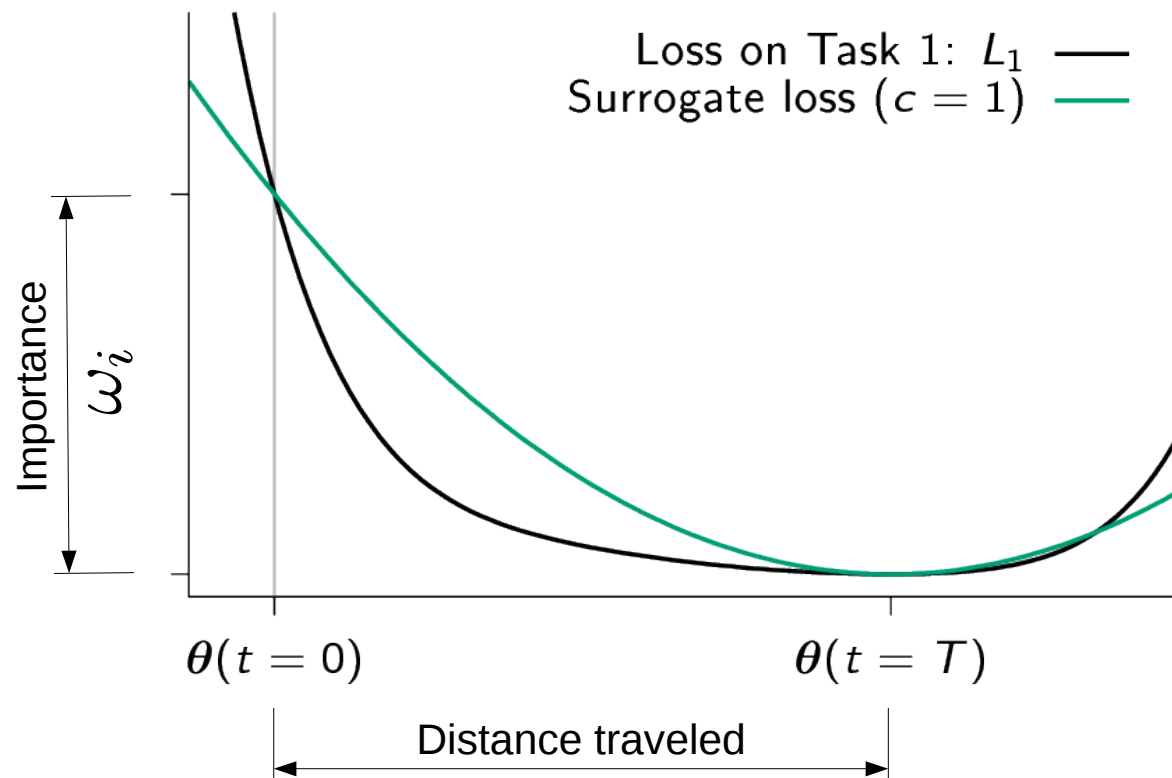
$$L(\theta) = L_2(\theta) + c \sum_i \Omega_i (\theta_i - \theta_{1,i}^*)^2$$



Leveraging per-parameter importance for continual learning

$$L(\theta) = L_2(\theta) + c \sum_i \Omega_i (\theta_i - \theta_{1,i}^*)^2$$

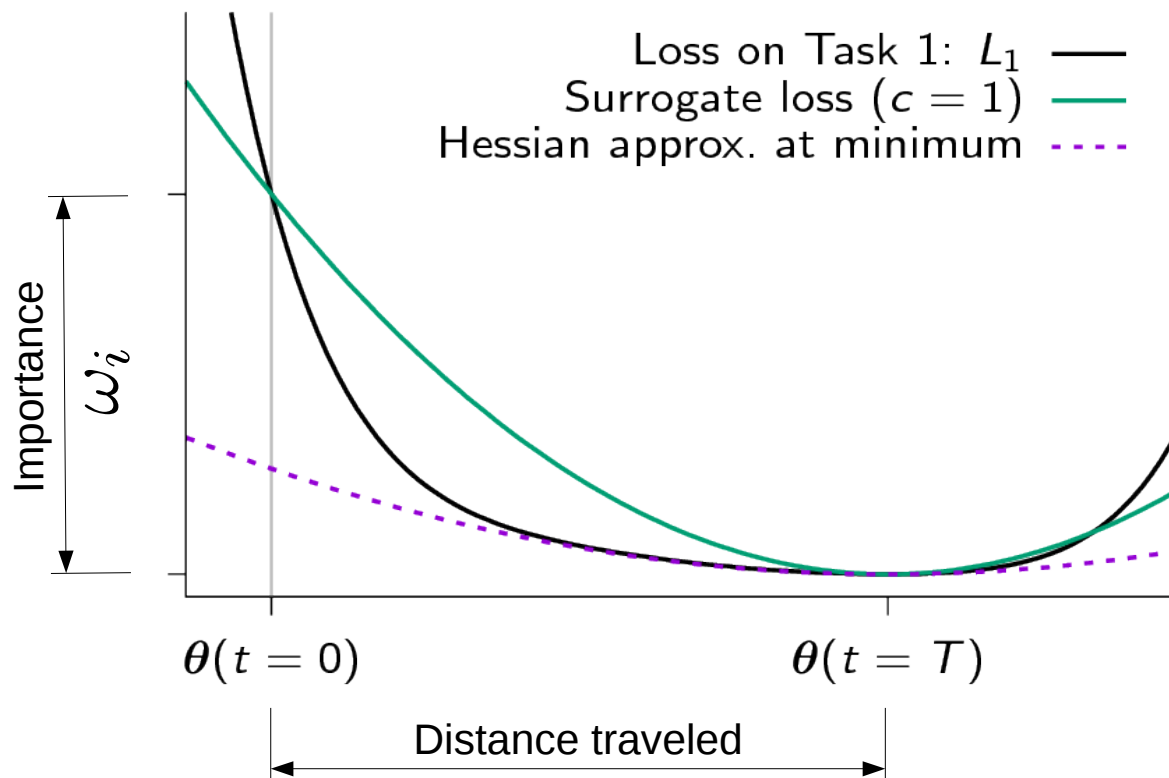
$$\Omega_i \equiv \frac{\omega_i}{(\Delta_i)^2 + \epsilon}$$



Leveraging per-parameter importance for continual learning

$$L(\theta) = L_2(\theta) + c \sum_i \Omega_i (\theta_i - \theta_{1,i}^*)^2$$

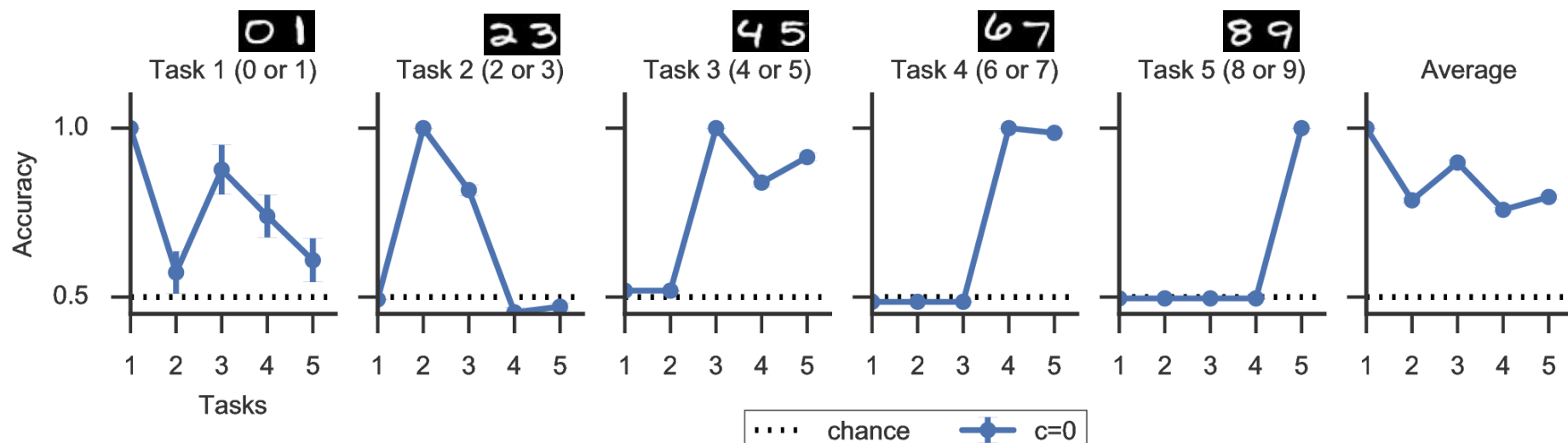
$$\Omega_i \equiv \frac{\omega_i}{(\Delta_i)^2 + \epsilon}$$



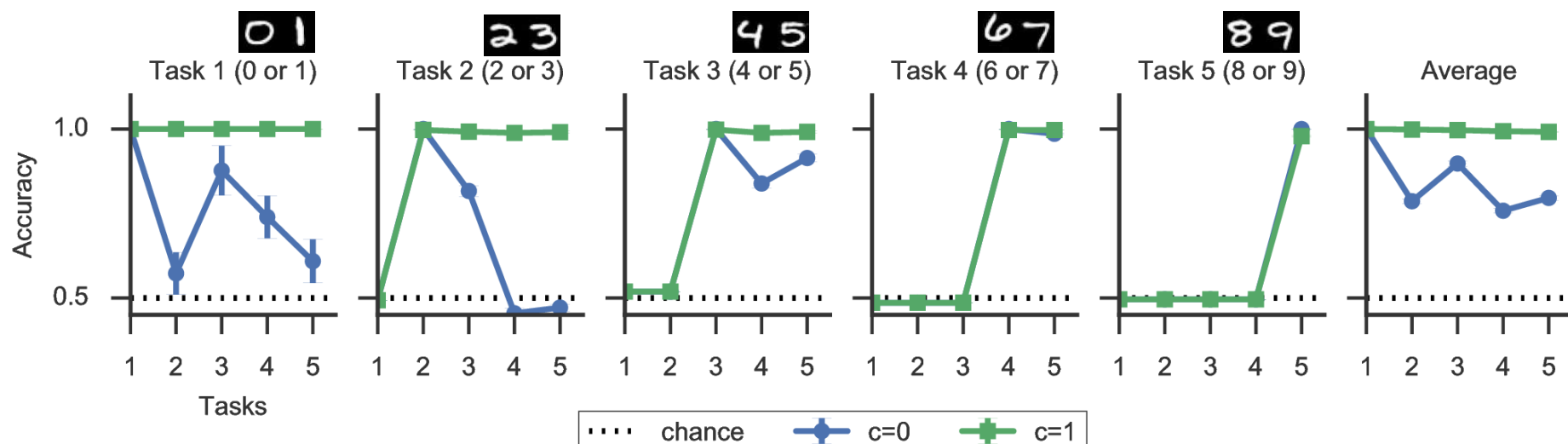
- Surrogate loss
 - Per-parameter importance
 - Distance traveled
- Different from local approximation
- Recovers Hessian for simple quadratic problems

Experiments

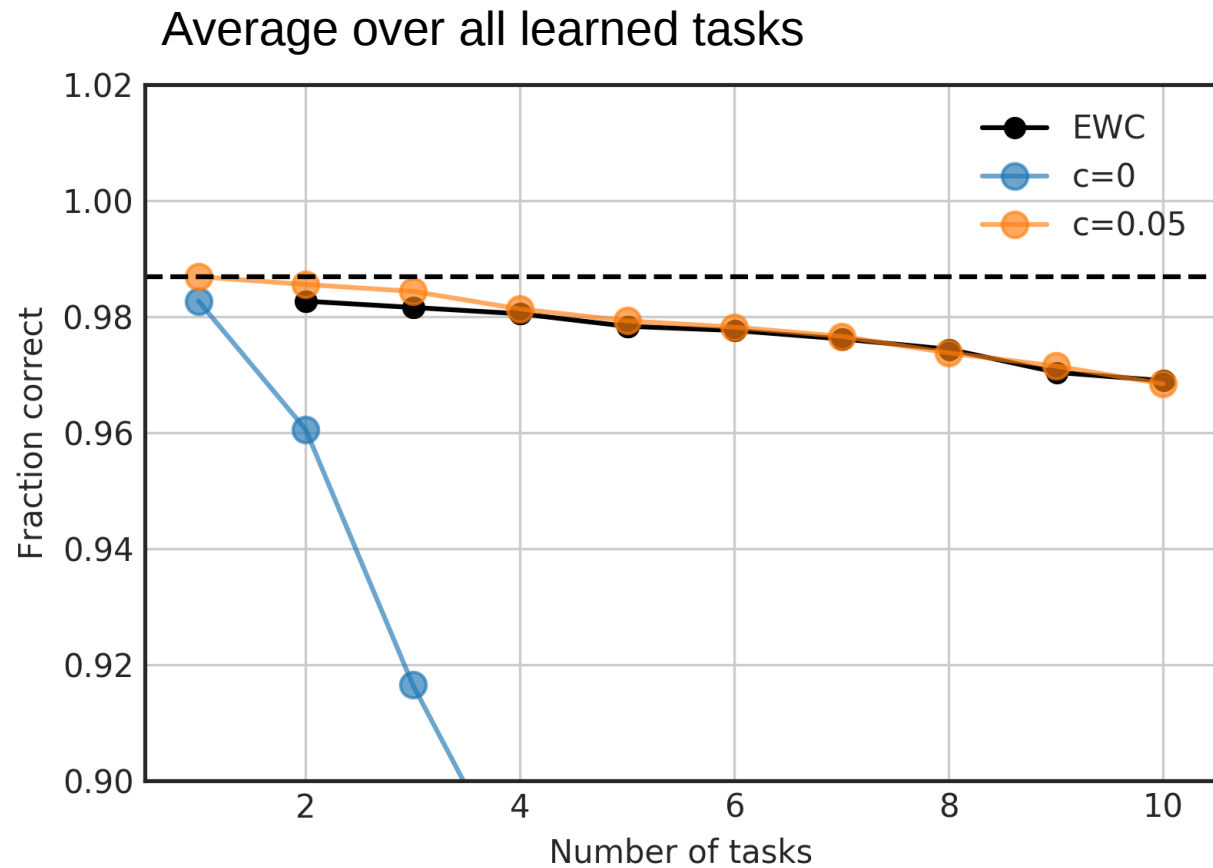
Catastrophic forgetting (split MNIST)



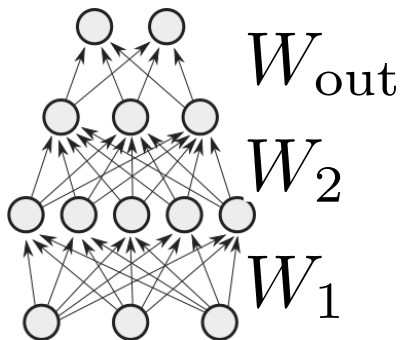
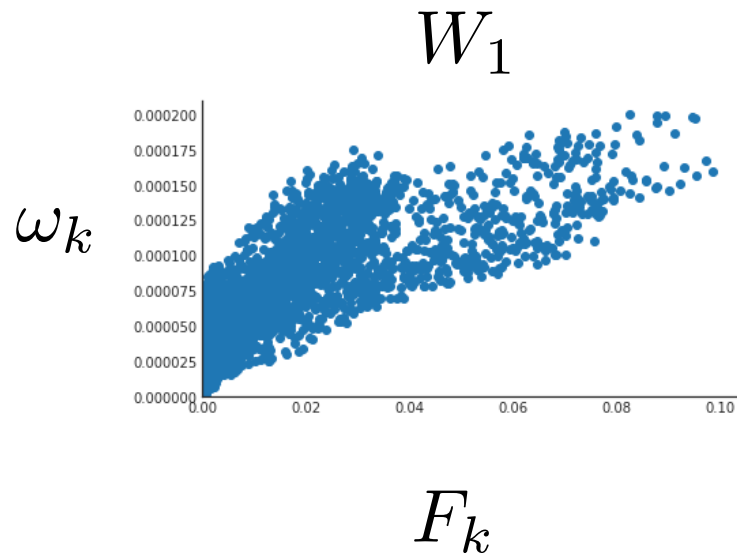
Catastrophic forgetting (split MNIST)



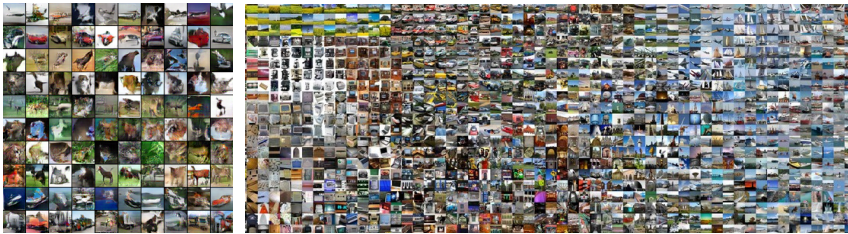
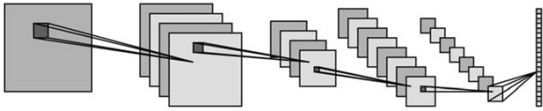
Permuted MNIST



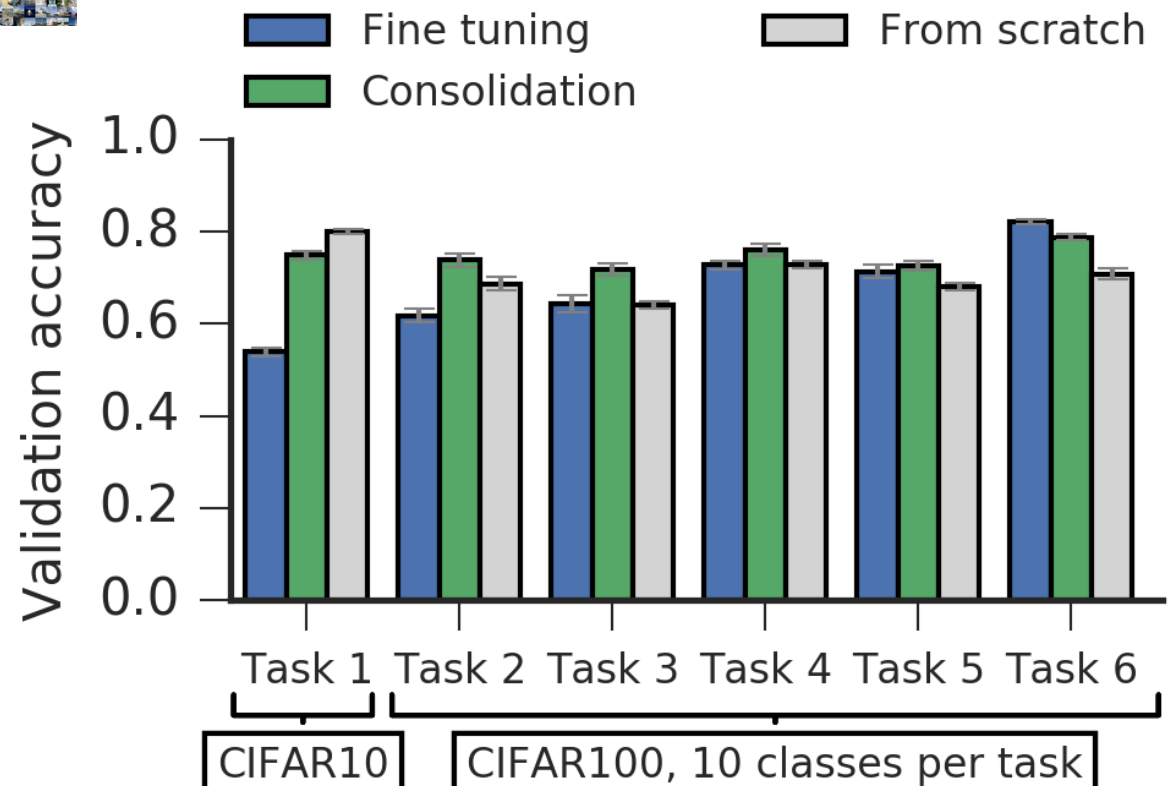
Fisher and our importance measure are correlated



Works for CNNs: CIFAR10/100



After training on all tasks



Summary

- Individual synapses can estimate their importance as contribution to changes in loss
- They can do this on-line by efficiently computing the path integral over the entire parameter trajectory
- Exploiting this information intelligently
 - Alleviates catastrophic forgetting
 - Yields better generalization

Thanks

Poster: #46

Code: <https://github.com/ganguli-lab/pathint>

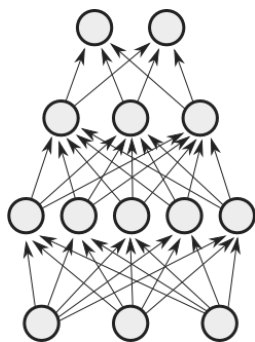
Funding:



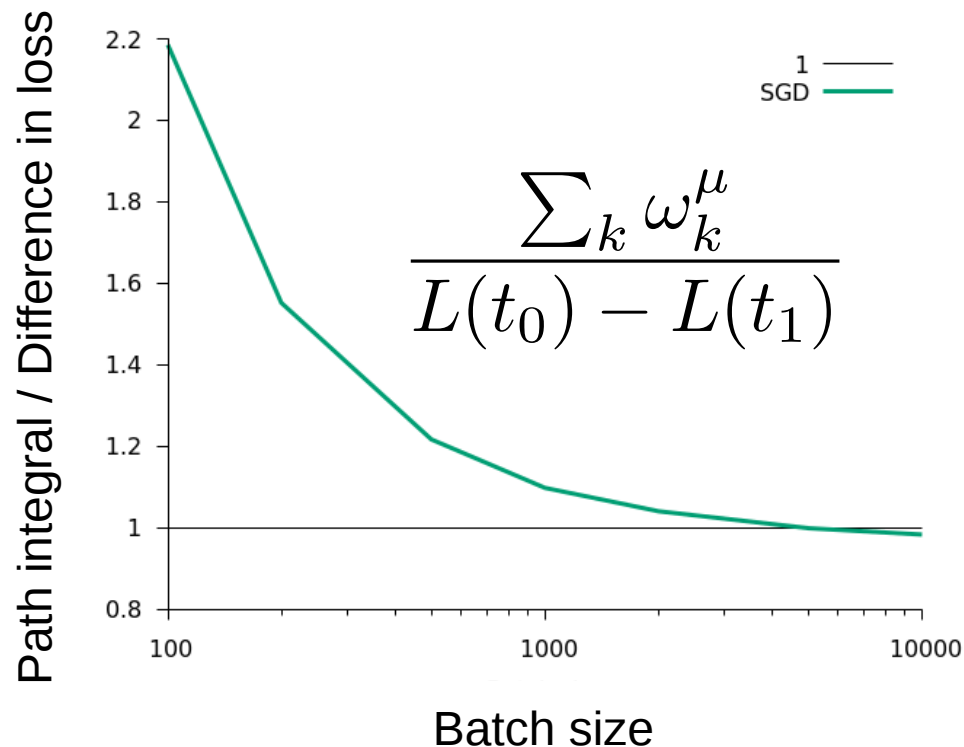
SWISS NATIONAL SCIENCE FOUNDATION



Sanity check: $-\sum_k \omega_k^\mu$ corresponds to difference in loss

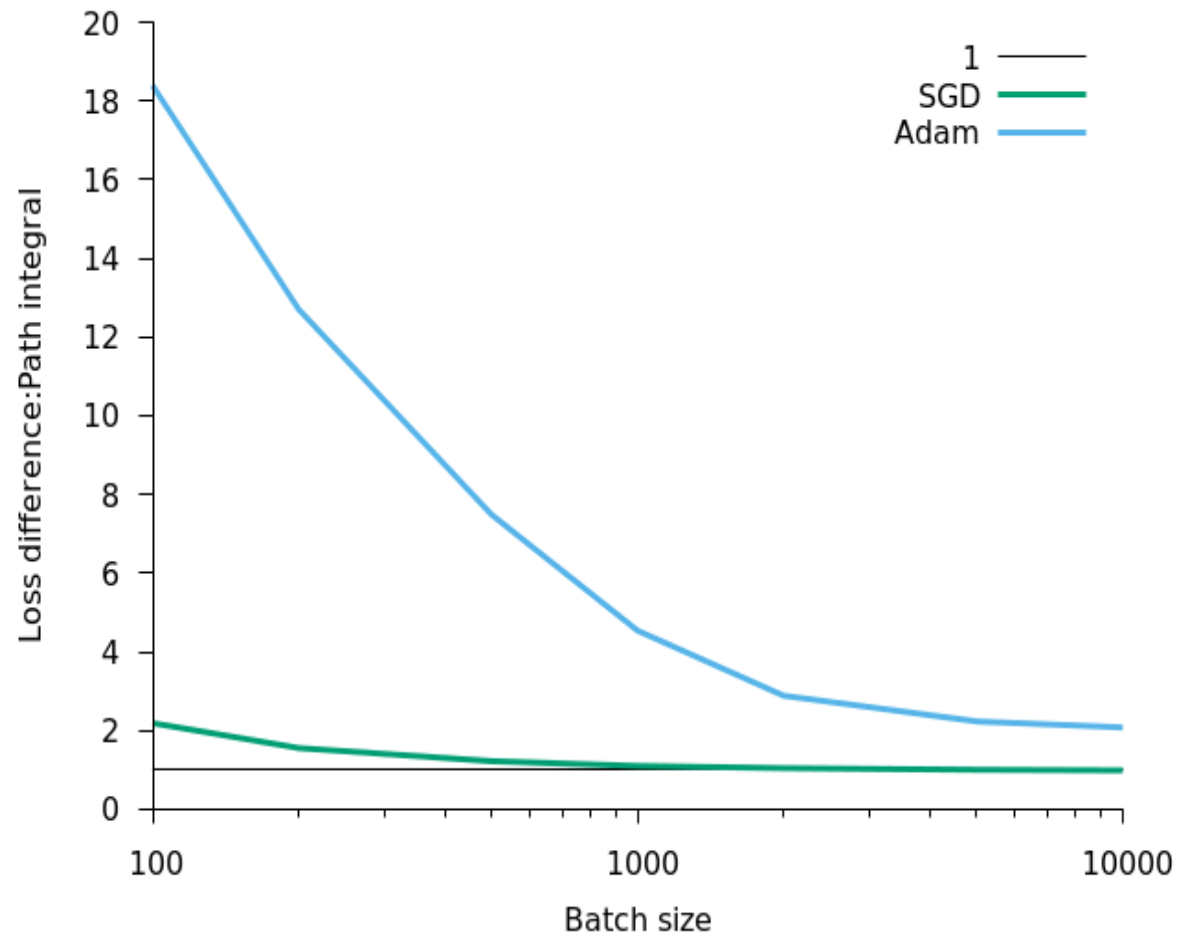


- MLP, MNIST
- 5.6M parameters

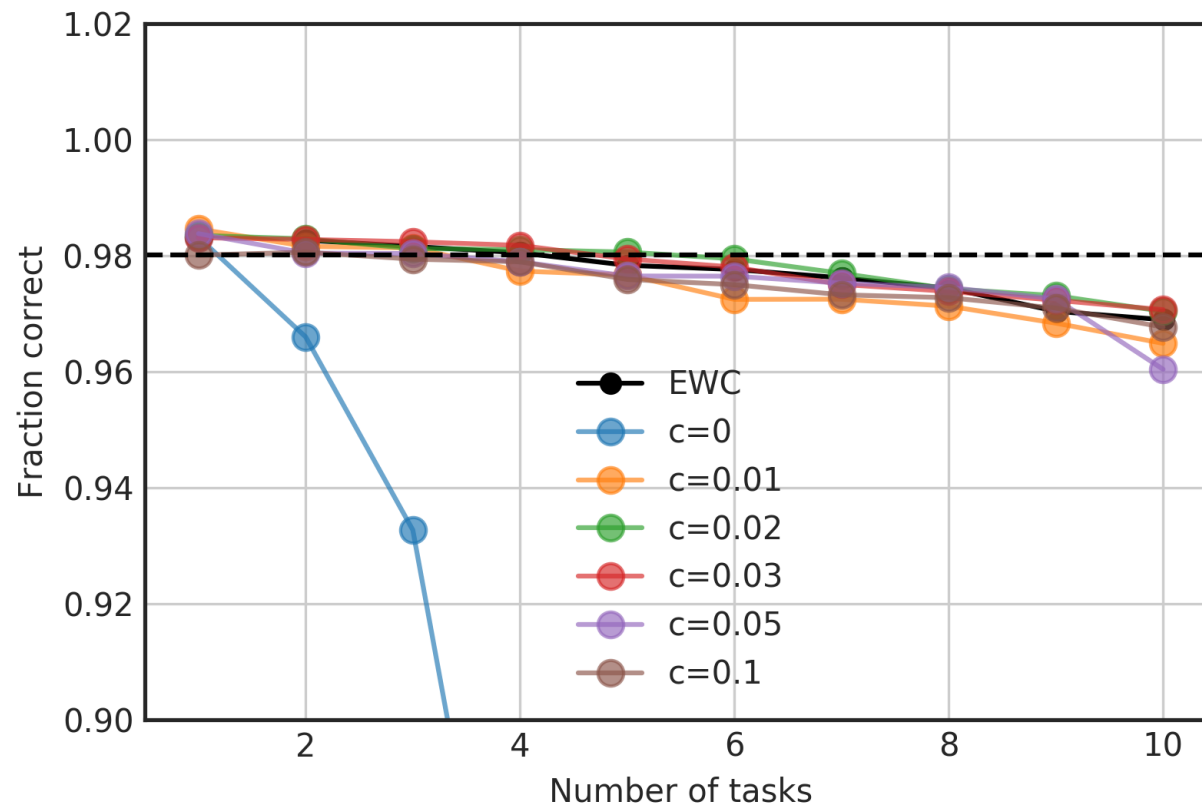


- Deviation due to noise from SGD
- Can be corrected with a multiplicative correction

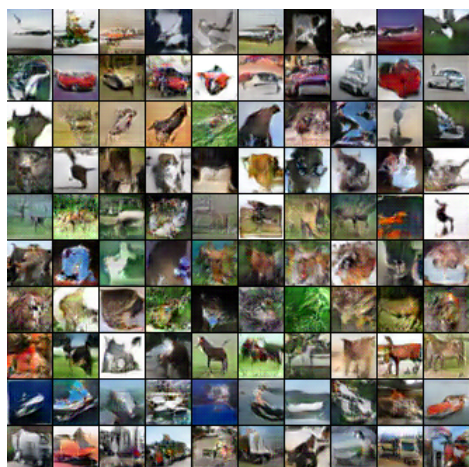
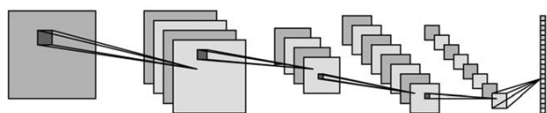
How well is the path integral approximated by SGD&Adam



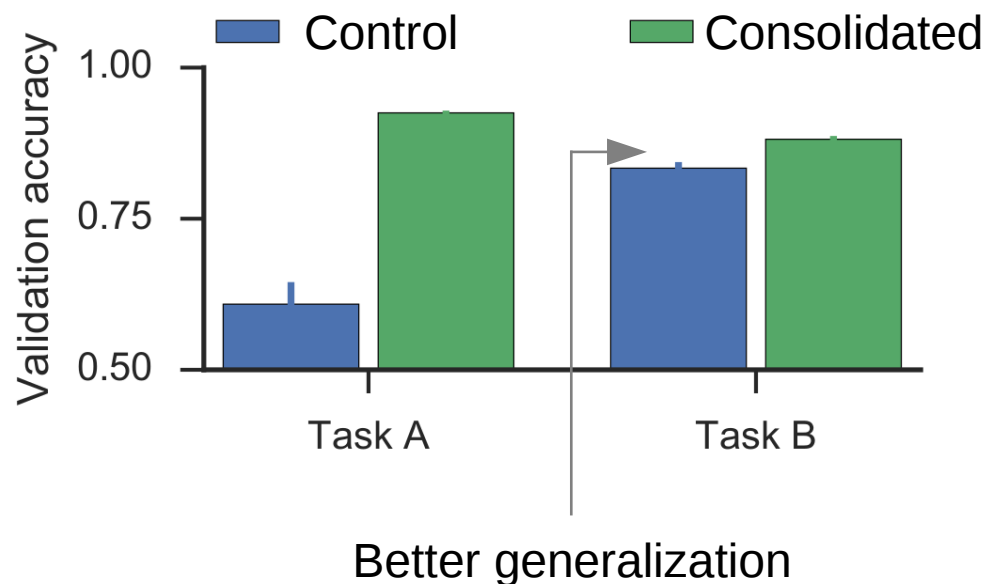
Permuted MNIST



Works for CNNs: Split CIFAR10

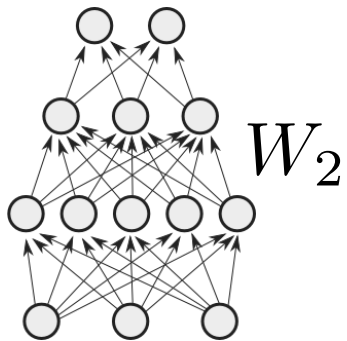


After training on Task A & B:



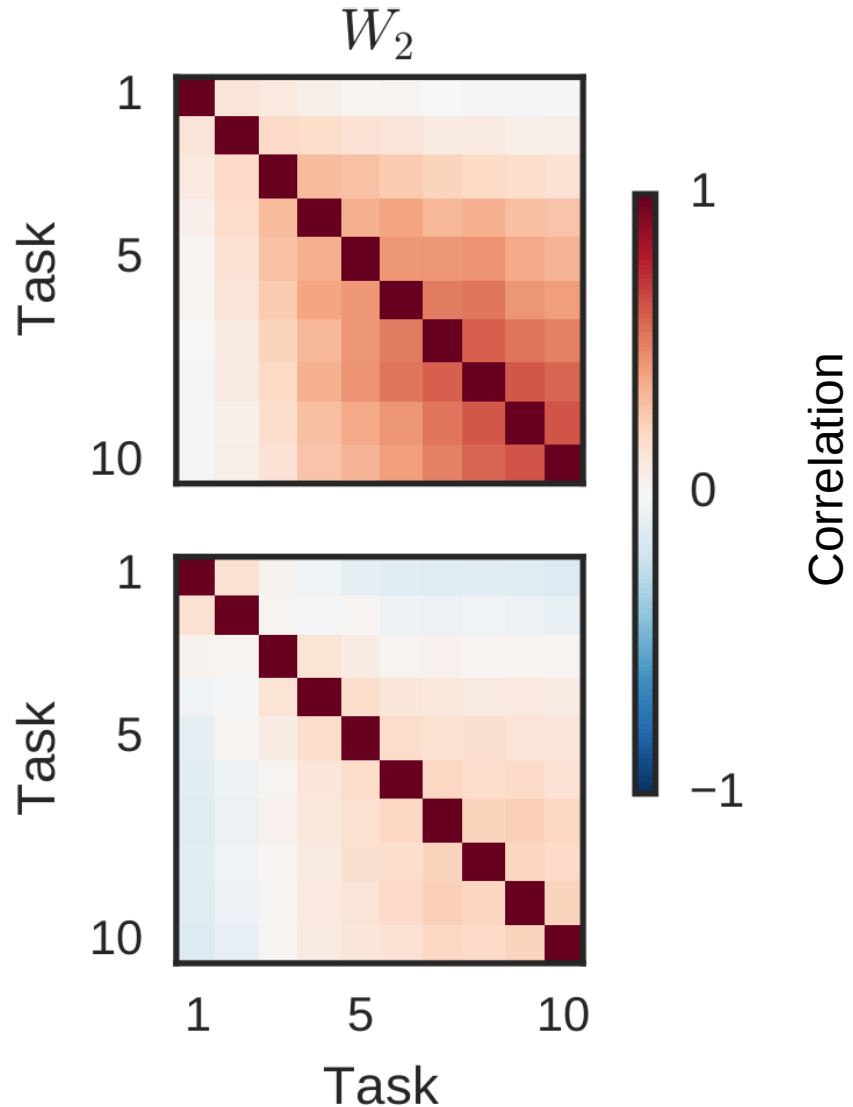
Task importance less correlated in hidden layers

Correlation matrix of the ω_k^μ



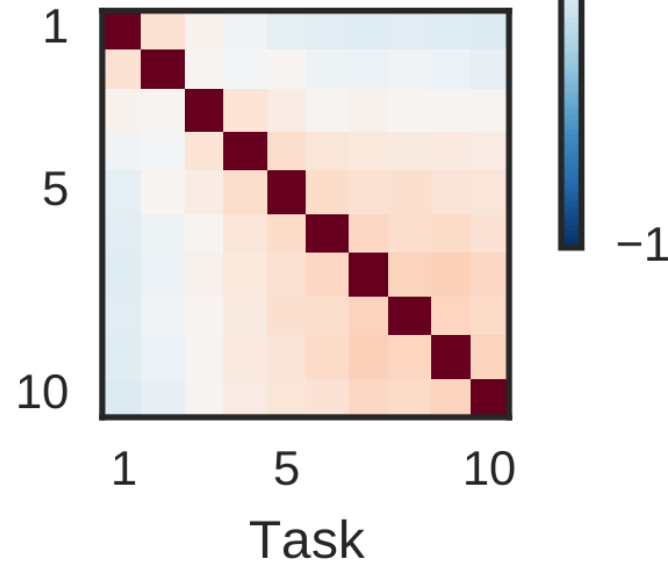
No consolidation

$$c=0$$

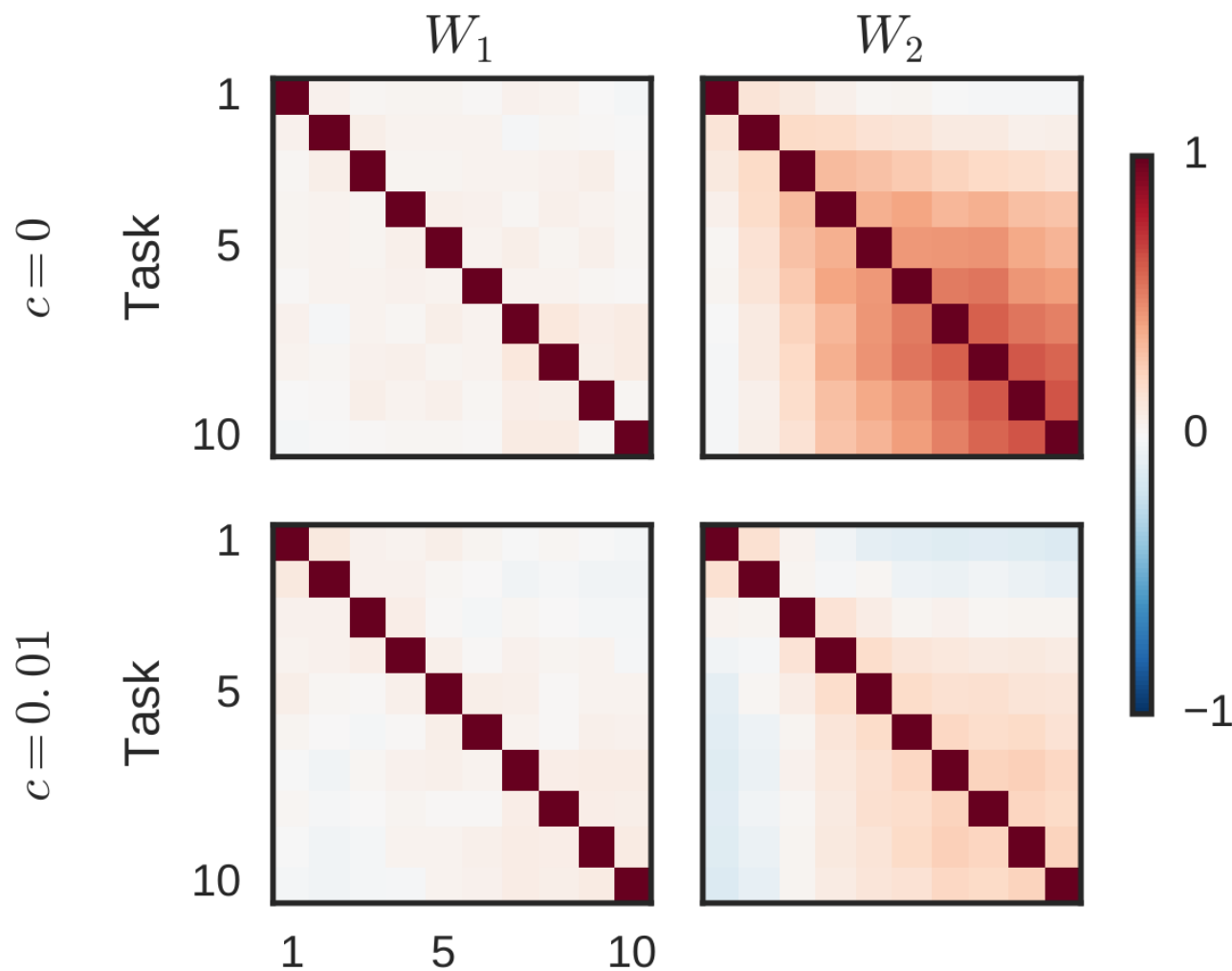


With consolidation

$$c=0.01$$

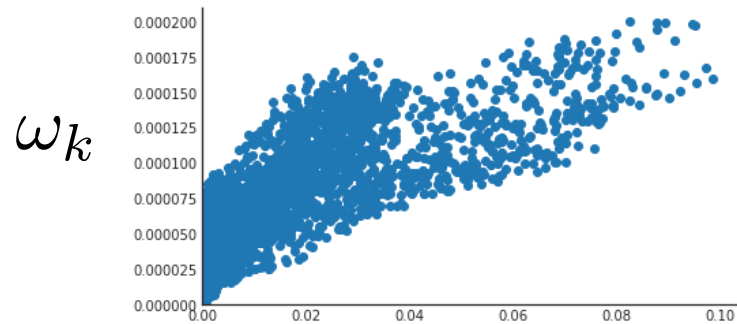


Task importance less correlated in hidden layers

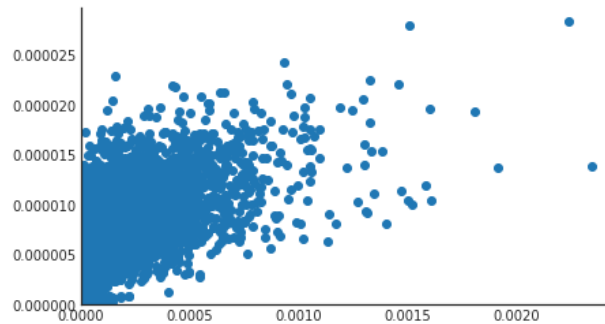


Fisher and our importance measure are correlated

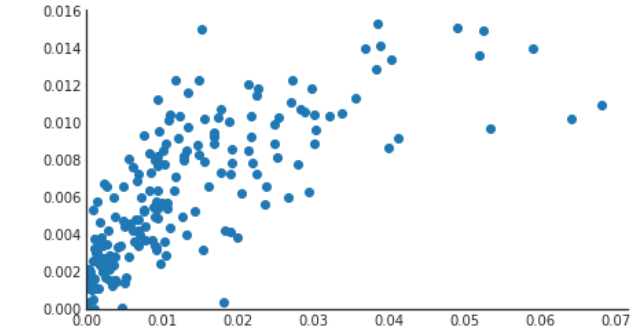
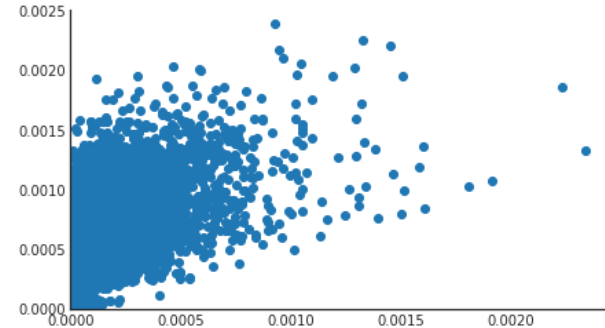
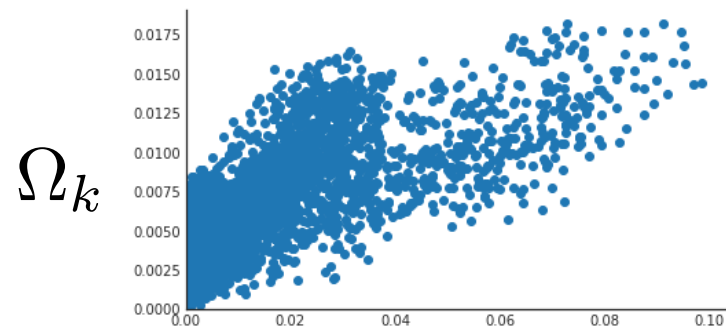
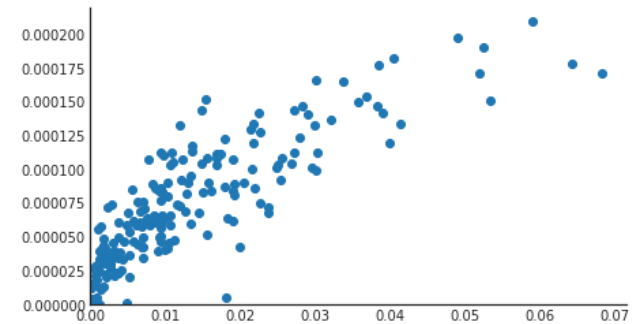
Layer 1



Layer 2



Layer 3



F_k

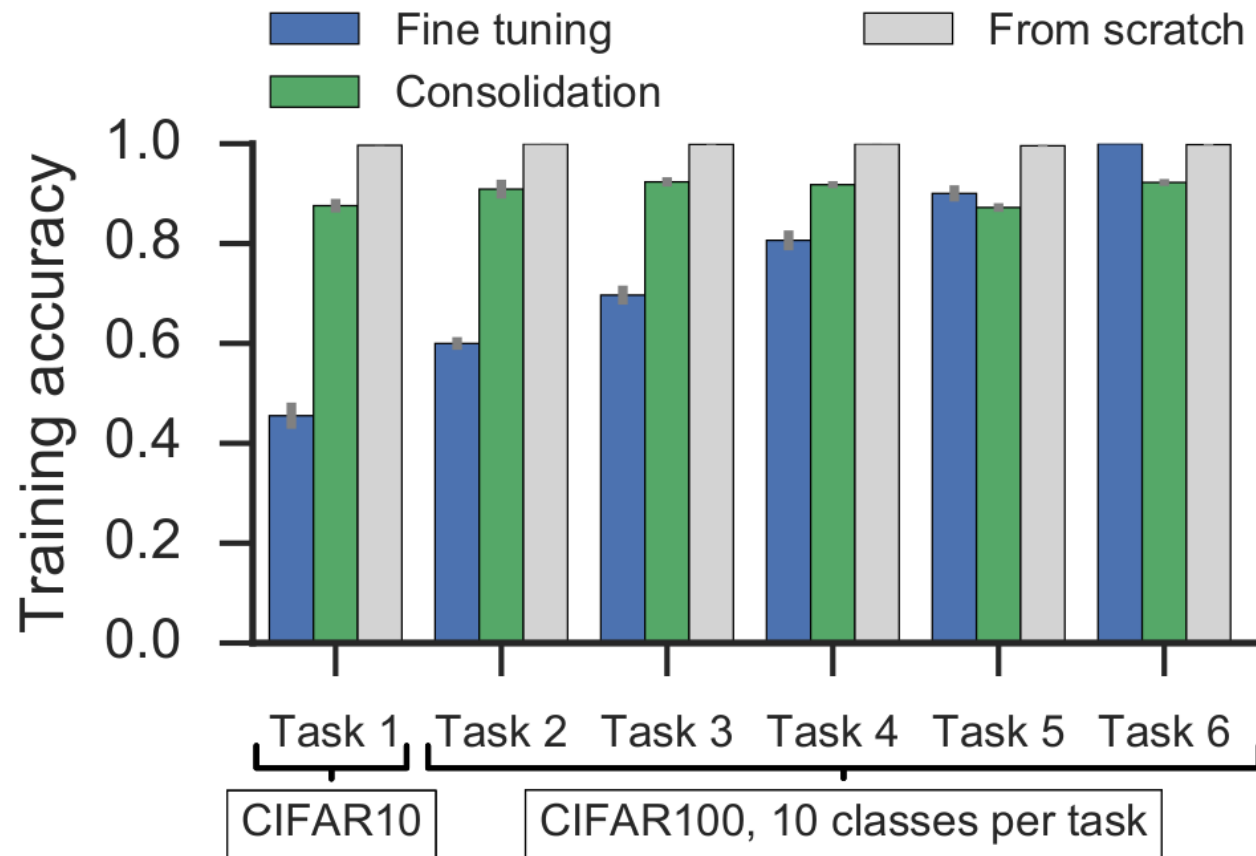
F_k

F_k

Previous approaches

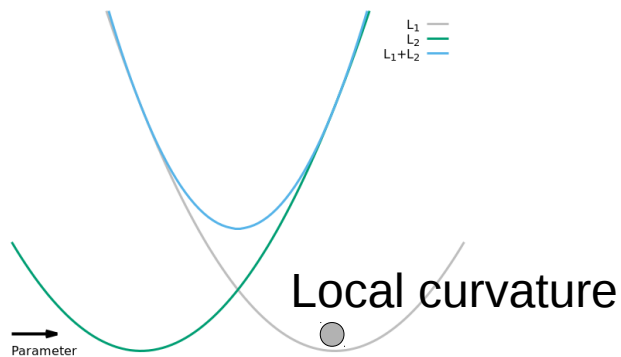
- **Architectural:** modify architecture to prevent forgetting
Specific nonlinearities (Goodfellow et al., 2013; Srivasta et al., 2013), progressive nets (Rusu et al., 2016), fine tuning (Donahue et al., 2014)
con: architectural complexity grows with tasks
- **Functional:** regularize activations or outputs of network
LwF (Li & Hoiem, 2016), LFL (Jung et al., 2016)
con: additional memory and computation to compare activations
- **Structural:** regularize parameters of network
Elastic weight consolidation (Kirkpatrick et al., 2017)
con: expensive to compute weights for regularization penalty

Training Error Split CIFAR10/100

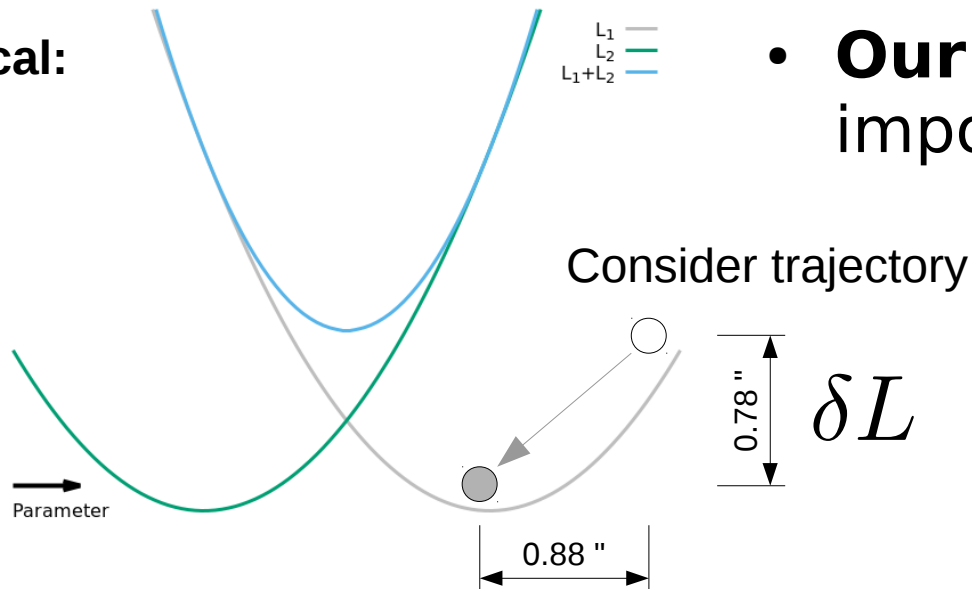


How to measure per-parameter importance: Local vs non-local

Local:



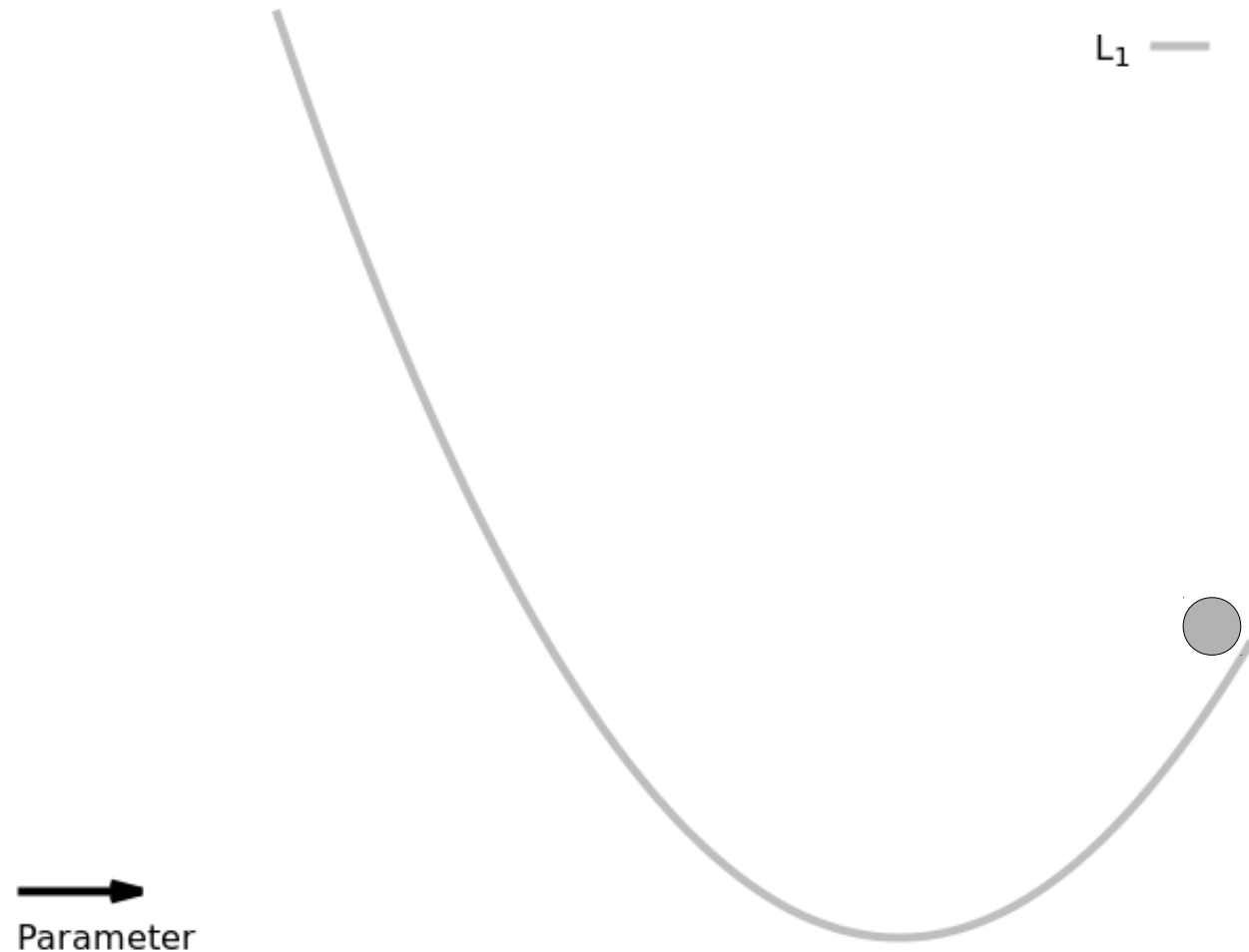
Non-local:



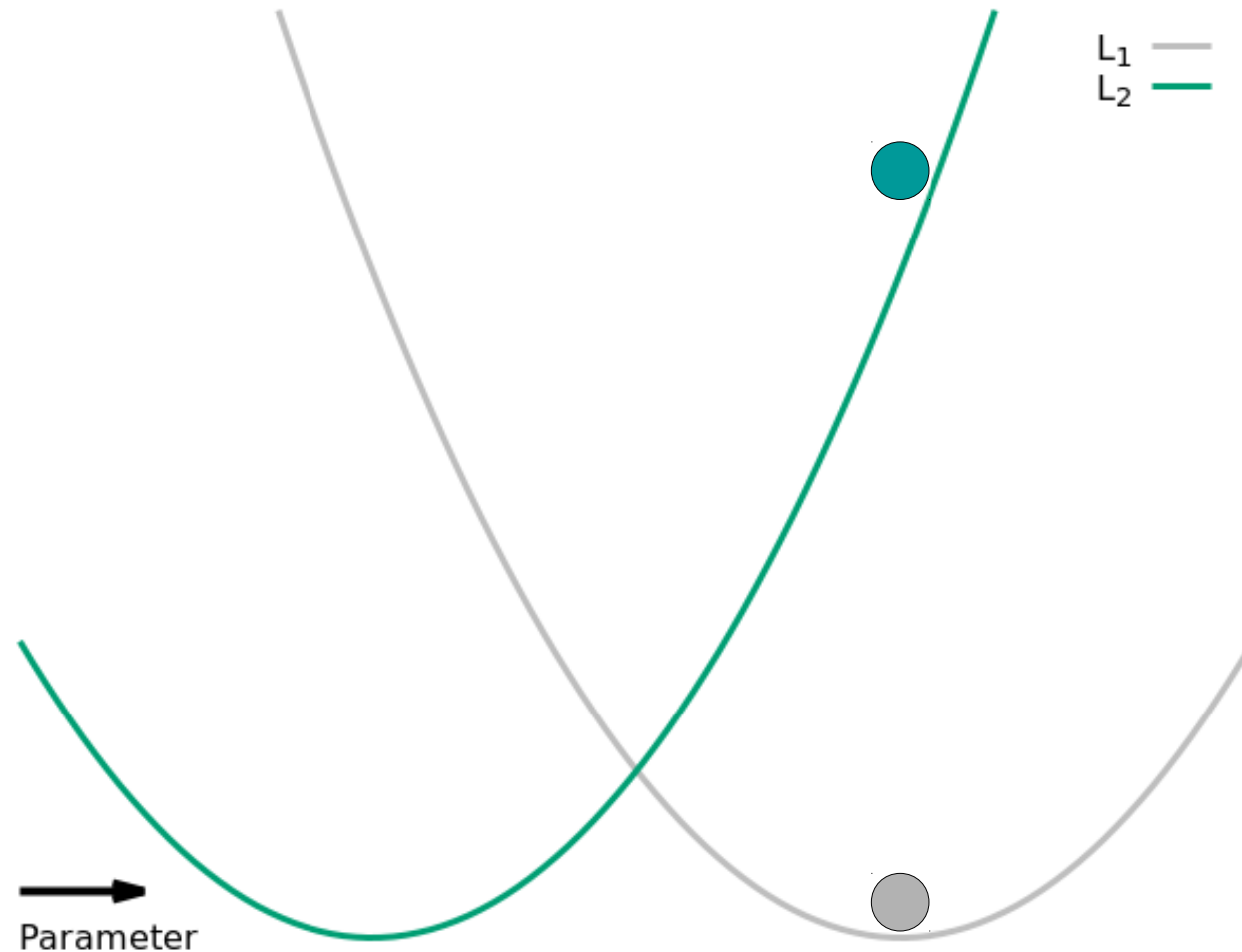
- **Our approach:** Estimate importance from trajectory

Need per-parameter contribution to changes in total loss L

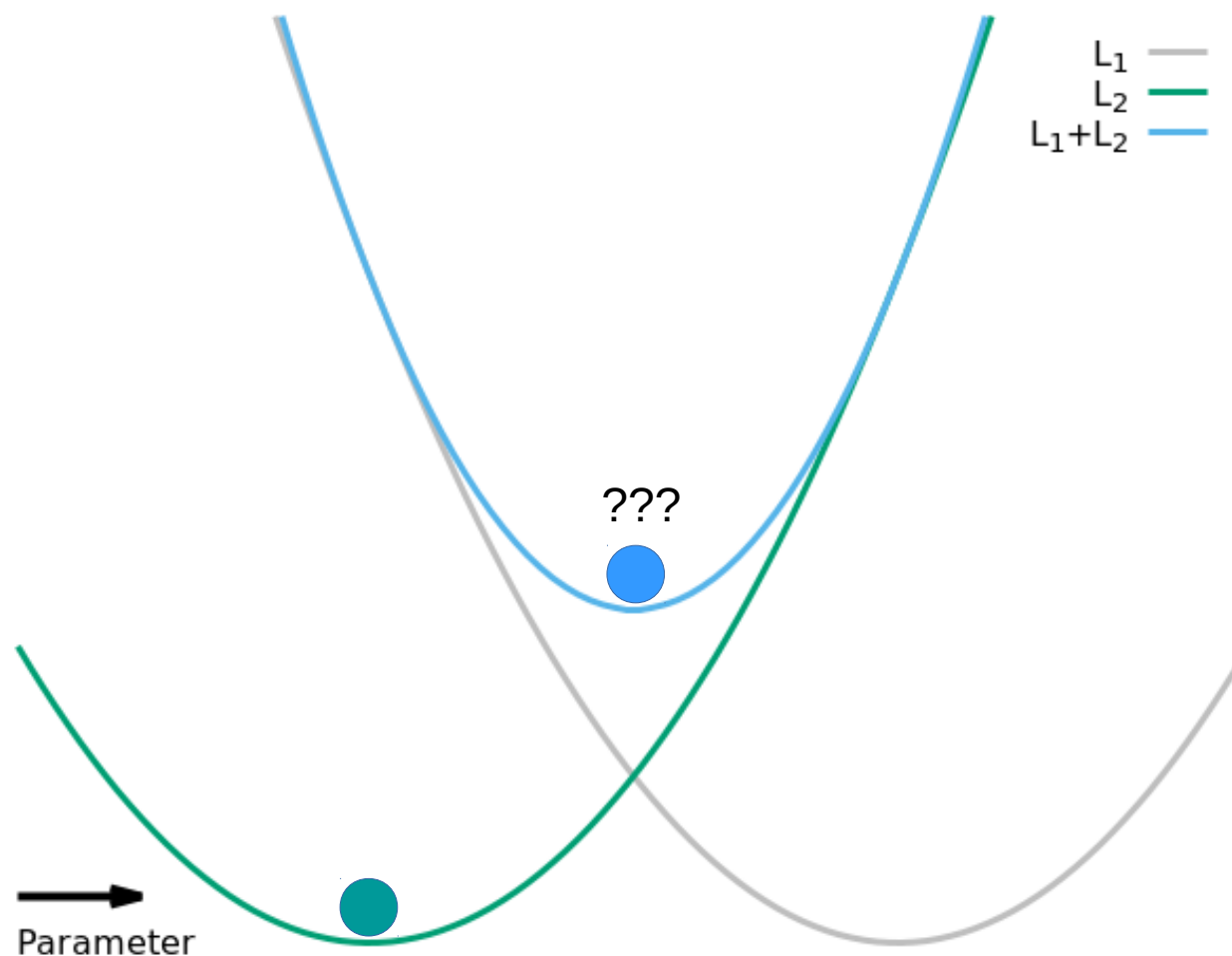
Problem: Catastrophic forgetting



Problem: Catastrophic forgetting



Problem: Catastrophic forgetting



$$L(\theta) = L_2 + L_1^{\text{approx}}$$